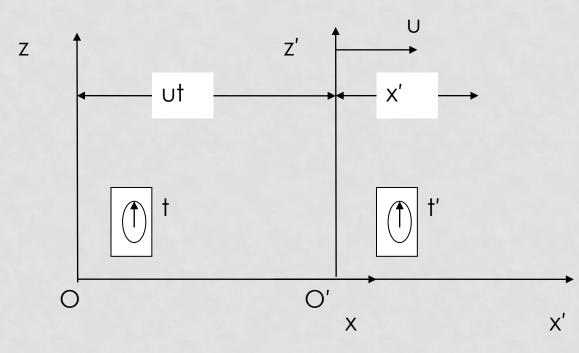
- Again consider the transformation problem.
- The required transformation consists of equations allowing us to calculate the primed set of numbers in terms of the unprimed set or vice versa.
- The Lorentz transforms replace the Galilean transforms of position and time.

$$(x', y', z'; t')$$

- The Lorentz transformations will be proved at a later.
- Again consider the case,



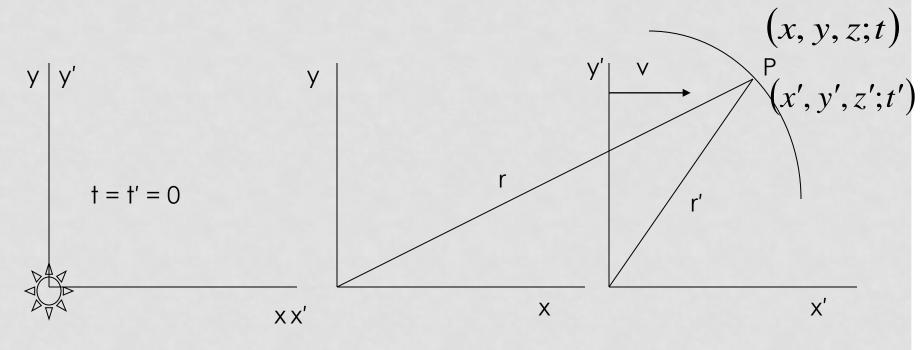
• The Lorentz transformations for position and time are:

$$x = (x' + vt')\gamma$$
$$t = \gamma \left(t' + \frac{vx'}{c^2}\right)$$
$$y = y' \quad z = z'$$

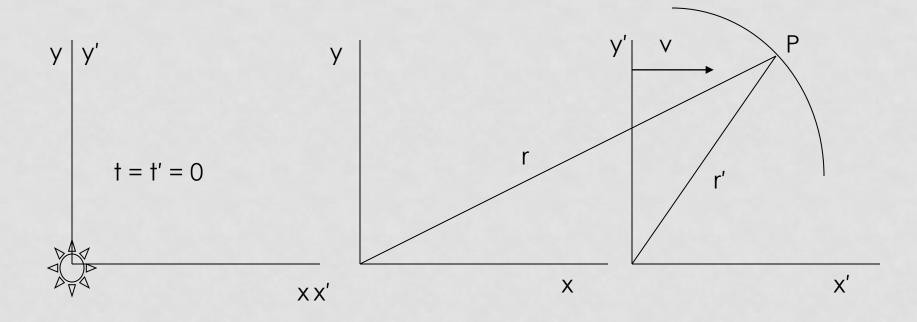
• The inverse of these equations give:

$$x' = (x - vt)\gamma$$
$$t' = \gamma \left(t - \frac{vx}{c^2}\right)$$
$$y' = y \quad z' = z$$

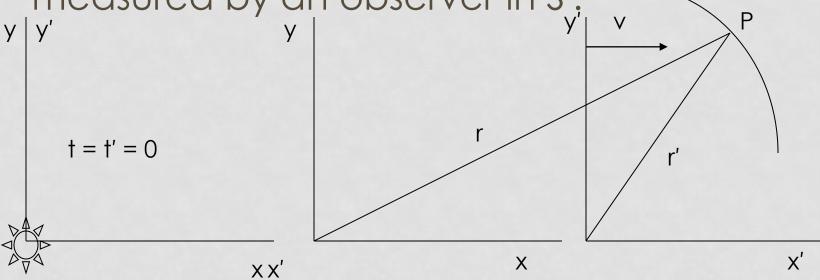
- The transformation equations are valid for all speeds < c.
- Consider a flash bulb attached to S' that goes off,



• At the instance it goes off the two frames coincide. At some later time the wavefront is at some point P.

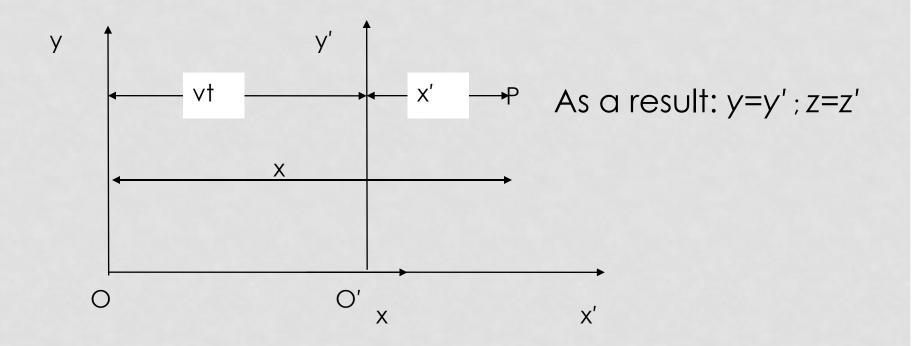


- r: distance to a point on the wavefront measured by an observer in S.
- r': distance to a point on the wavefront measured by an observer in S'.



r=ct ..(1) Stationary Frame
r'=ct' ..(2) Moving Frame

• For simplicity, the general problem is stated so that the motion of P is along the x-x' axis.



• Radius of a sphere is $r^2 = x^2 + y^2 + z^2$ in the S frame and similarly $(r')^2 = (x')^2 + (y')^2 + (z')^2$ in the S' frame.

$$x^{2} + y^{2} + z^{2} = c^{2}t^{2} \qquad ..(3)$$
$$(x')^{2} + (y')^{2} + (z')^{2} = c^{2}(t')^{2} \qquad ..(4)$$

• Substituting is y = y'; z = z' into the previous equations and subtracting we get that,

$$x^{2} - (x')^{2} = c^{2}t^{2} - c^{2}(t')^{2}$$
$$x^{2} - c^{2}t^{2} = (x')^{2} - c^{2}(t')^{2} \qquad ..(5)$$

- We know that in the stationary frame, the distance travelled is given by
- x = vt ...(6) • In the stationary frame, the distance travelled is

$$x' = 0 \qquad \dots (7)$$

• We know that in the stationary frame, the distance travelled is given by

x = vt ...(6) • In the stationary frame, the distance travelled is

• Using equations 5,6,7 we can show that, x' = 0 ...(7)

$$x' = (x - vt)\gamma \quad ..(8) \qquad t' = \left(t - \frac{v}{c^2}x\right)\gamma \quad ..(9)$$

• Summary:

$$x' = (x - vt)\gamma$$
$$t' = \gamma \left(t - \frac{vx}{c^2}\right)$$
$$y' = y \quad z' = z$$

• Summary:

$$x' = (x - vt)\gamma$$
$$t' = \gamma \left(t - \frac{vx}{c^2}\right)$$
$$v' = v \quad z' = z$$

• The Lorentz transformations can be verified by substituting equations 8,9 into the RHS of equation 5.

 To produce the Lorentz transformations for primed frame to the unprimed frame we substitute v with – v.

$$x = (x' + vt')\gamma$$
$$t = \gamma \left(t' + \frac{vx'}{c^2}\right)$$
$$y = y' \quad z = z'$$

• For v << c, the Lorentz transformations reduce to the Galilean transformations. When v << c; v/c <<1 and $\cdot \frac{v^2}{c^2} <<1$

- Solution:
- The question requires us to transform from the unprimed to the primed! Therefore use,

$$x' = (x - vt)\gamma$$
$$t' = \gamma \left(t - \frac{vx}{c^2}\right)$$
$$y' = y \quad z' = z$$